

1. Demonstrate how to evaluate  $\int \cos^2(\theta) d\theta$  using integration by parts.

2. **Particle, the Dog:**

My dog, Particle, and I like to walk on the Cartesian plan. Like most dogs, Particle walks further than I do, even though we start and end in the same places. Unlike most dogs, Particle walks along a path described by a sine curve.

As I walk along the  $x$ -axis, Particle moves along the curve  $y = \sin x$ , so that her  $x$  is the same as mine. For now, your goal is to develop distance function,  $P(x)$ , that takes a value of  $x$  and gives the "distance" Particle has walked along the sine curve from her starting point at the origin.

- (a) Develop a *distance element*,  $dP$ , for computing Particle's distance. Use this to come up with a method to obtain how far Particle has walked from the origin when I am at any point  $x$ . Be sure your  $dP$  is ready to be integrated. (Discuss what does this means.)
- (b) Use your  $dP$  and an integral to define our function,  $P(x)$ . (You need not try to express  $P(x)$  without an integral.)
- (c) If I am walking along the  $x$ -axis at a rate of one unit per minute, what is Particle's speed along the curve as a function of  $t$ ?
- (d) What are Particle's maximum and minimum speeds, and where do they occur?