

1. What does the *Fundamental Theorem of Calculus (Part 1)* say?

2. Evaluate $A'(x)$ when:

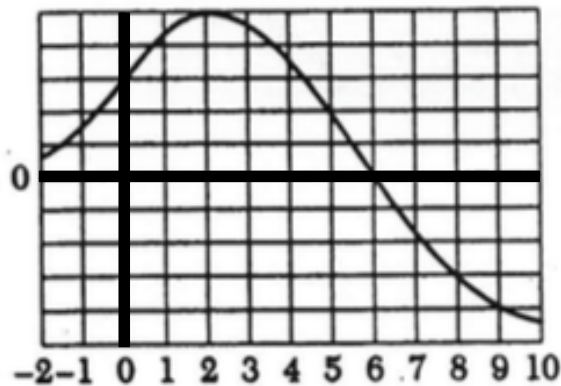
(a) $A(x) = \int_0^x t^2 dt$

(b) $A(x) = \int_3^x t^3 dt$

(c) $A(x) = \int_x^5 \ln(t) dt$

(d) $A(x) = \int_3^{x^2} 7^t dt$

3. Let $A_f(x) = \int_0^x f(t) dt$ where $f(x)$ is the function in the graph.



- (a) Which is larger: $A_f(1)$ or $A_f(5)$? Justify your answer.
- (b) Which is larger: $A_f(7)$ or $A_f(10)$? Justify your answer.
- (c) Which is larger: $A_f(-2)$ or $A_f(-1)$? Justify your answer.
- (d) Where is $A_f(x)$ increasing?
- (e) Explain why $A_f(x)$ has a stationary point at $x = 6$. Is this a local minimum or a local maximum?
- (f) Let $F(x) = \int_{-2}^x f(t) dt$. Explain why $A_f(x) = F(x) + C$ where C is a negative constant.
- (g) The five numbers $A_f(4) - A_f(3)$, $A_f(5) - A_f(4)$, $A_f(6) - A_f(5)$, $A_f(7) - A_f(6)$, and $A_f(8) - A_f(7)$ can each be interpreted as the slope of a secant line of $A_f(x)$. Explain.
- (h) Explain how to use the graph of $f(x)$ to determine the concavity of $A_f(x)$ on the interval $[3, 8]$.
- (i) Rank the five numbers 0 , $A_f(-1) - A_f(-2)$, $A_f(0) - A_f(-1)$, $A_f(1) - A_f(0)$, and $A_f(2) - A_f(1)$ in increasing order. Explain your reasoning.

4. Revisit question 3. Answer each subquestion using *only* the Fundamental Theorem of Calculus. [The word *area* cannot be used in any of your explanations.]
5. You work for Acme Can Company. A standard ACC juice can (which you can assume to be a cylinder) has a volume of 355 cm^3 .
- (a) Find the dimensions (radius r and height h) that minimize the surface area of the can.
 - (b) How can you check your answer? Do it.
6. A rectangle has its base on the x -axis, a vertex on the y -axis, and a (different) vertex on the curve defined by $y = e^{-x^2}$.
- (a) What choice of vertices gives the largest area?
 - (b) Show that one of the vertices found in part (a) is at an inflection point of the curve.